

geometric mean for $m \rightarrow 0$ as follows:

$$\hat{\chi}(t+p) = \sqrt[M]{\prod_{i=1}^M \chi(k_i+p)}$$